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Solute segregation in materials with grain boundaries (GBs) has emerged as a popular method to thermody-

namically stabilize nanocrystalline structures. However, the impact of varied GB crystallographic character on solute segregation has never been thoroughly examined. This work examines Co solute segregation in a dataset

of 7272 Al bicrystal GBs that span the 5D space of GB crystallographic character. Considerable attention is

paid to verification of the calculations in the diverse and large set of GBs. In addition, the results of this work

are favorably validated against similar bicrystal and polycrystal simulations. As with other work, we show that Co atoms exhibit strong segregation to sites in Al GBs and that segregation correlates strongly with GB

energy and GB excess volume. Segregation varies smoothly in the 5D crystallographic space but has a complex



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Full length article Grain boundary solute segregation across the 5D space of crystallographic character

ABSTRACT

landscape without an obvious functional form.

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1. Introduction

Solute atoms in polycrystalline materials with grain boundaries (GBs) may stay in the bulk, diffuse to the surface, or segregate to the GB, among other behaviors such as forming precipitates. When solute atoms segregate, they often remain in the GB network due to both kinetic mechanisms and thermodynamic stabilization. Some examples of kinetic mechanisms are solute drag that slows GB mobility [1] and solute pinning that prevents GB mobility under external driving forces [2]. Thermodynamic stabilization involves lowering the Gibbs free energy of a GB interface by the presence of the solute atom [3,4], and is described in a theoretical framework developed by Weissmüller [5,6]. Thermodynamic stabilization can be utilized to engineer materials with greater hardness than a pure material even at elevated temperatures (e.g., in [3,7–9]) due to the Hall-Petch effect that causes greater hardness with smaller grain sizes [10,11]. A recent review of thermodynamic stabilization is given in [12].

While a variety of models for segregation energy exist [13], simple effective segregation energy models of solute segregation [14] were derived from experimentally determined values and are still often used to predict solute concentration at GBs and in larger mesoscale models [15–20]. However, such models violate the third law of thermodynamics [21], do not account for the effects of GB character on the system, and are insufficient to describe experimental behavior [22–24],

in particular of strong segregation to specific atom sites (e.g., in the Co-Al-W system [25]).

Recently, models that are informed by simulated data have been developed to address such issues. GB solute segregation has been examined in the dilute limit in atomistic studies utilizing polycrystals [21,26-30] and bicrystals in small regions of the 5D GB space [31-36], as well as in first-principles [36-41] and experimental studies [42,43]. Some studies improve on the segregation energy calculations by including entropic and other effects in the atomistic simulations [30,44]. Others move beyond the dilute limit by considering solutesolute interactions [45], or multiple-solute interactions [46]. From these data, segregation models are often created using machine learning techniques [27,31,32], specifically to predict segregation energy of specific atom sites from their local environments. Recent reviews of computational modeling of solute segregation are given in [47,48]. Here, we highlight two recent and notable efforts to create more accurate segregation energy models based on segregation energy spectra, which permits enforcement of the third law of thermodynamics [21].

Huber et al. created a small dataset of densely sampled $\Sigma 5$ coincident site lattice (CSL) Al bicrystal GBs and calculated segregation energy spectra for 6 different solute types to inform machine learning models for solute segregation at the atomic level [31]. They found that a thorough sampling of the 5D space of GB crystallographic character was necessary for the creation of a segregation energy spectrum that

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informs a model more accurate than the rudimentary effective segregation energy model. Wagih et al. [28] also point out issues with using an effective segregation energy for solute concentration models, demonstrated by the bimodal spectrum of segregation energies in the Pd-H system due to the occupation of interstitial sites. In response, they created solute segregation spectra in polycrystals for use in segregation energy models by performing atomistic simulations of Mg in Al polycrystals [26]. This polycrystal approach creates one segregation energy spectrum for the entire dataset, rather than many small spectra that are concatenated to represent the dataset, as is necessary for bicrystal GBs. Wagih et al. used machine learning on these polycrystal spectra to inform 259 binary alloy system segregation models [27], as well as some quantum-accurate models [49].

Wagih et al. use polycrystal simulations in order to more fully capture the behavior of real materials, and they caution against using bicrystal simulations [26]. They suggest that only thorough samplings of bicrystal GBs in the 5D space of crystallographic character should be used for this purpose, promoting the work by Huber et al. in [31] as an example of sufficient sampling, albeit in a small subspace of the 5D space. Others have also noted the insufficiency of bicrystal GB simulations, such as Tucker et al. who use the strain functional description of atomic configurations to show that symmetric twist GBs (STGBs) cannot be used to represent polycrystals or amorphous structures [50]. Wagih et al. also present evidence that STGBs and low CSL GBs do not represent polycrystals generally [51].

In this work, we compute the segregation energy of 70 million Co atoms in 7272 Al bicrystal GBs from the Homer GB dataset [52,53]. The use of this dataset attempts to address most of the concerns raised about using bicrystal GB simulations to inform GB solute segregation models in [26,50,51] because it spans the 5D space of GB crystallographic character. It is also not limited to STGBs or low CSL GBs; it includes CSL values up to Σ 999. Additionally, the use of this dataset is a step towards examining the behavior of solute segregation across the entire GB space, which is noted as an important next step for the field [48], since segregation has been found to depend on GB character [54]. Co is used as a solute in this work because of its use in similar works [27,31], because Al-Co alloys can be used in a wide variety of applications [55], and because Co additions in small quantities can mitigate challenges in 3D printing of otherwise pure Al [56]. However, the methods and analysis described in this work could be repeated with other solvent-solute combinations. We verify and validate the resulting data, including direct comparisons to the works by Huber et al. in [31] and Wagih et al. in [27]. Finally, we examine the spectra using several techniques, including a statistical overview, a classification scheme, and reduction to a solute concentration for each GB, and we identify some subsets of GBs that deviate significantly from the mean solute concentration.

2. Methods

2.1. Theory of solute segregation

The segregation energy $E_{\rm seg}$ of an atom is defined as the energy difference between a solute atom and a solvent atom at the same site in the GB minus the same energy difference at a reference atom site located in bulk [13,26]. In this work, we examine the segregation of Co in Al, which is calculated according to:

$$E_{\text{seg}}^{\text{Co}_i} = \left(E_{\text{Co}}^i - E_{\text{Al}}^i\right) - \left(E_{\text{Co}}^{\text{ref}} - E_{\text{Al}}^{\text{ref}}\right) \tag{1}$$

where E_{Co}^i is the energy of a Co atom in the *i*th atomic site in a GB, E_{Al}^i is the energy of an Al atom in the *i*th atomic site, and E_{Co}^{ref} and E_{Al}^{ref} are the energies for a reference atom in bulk, far away from the GB.¹ All of these values are calculated at 0 K. In this formulation, segregation is energetically favorable for a site when $E_{seg}^{Co_i}$ is negative.

2.2. Solute segregation energy spectrum creation

In this work, segregation energy data is collected by substituting single Co atoms into Al GBs from a dataset created by Homer et al. [52, 53] which used the pure Al embedded atom method (EAM) potential from Mishin et al. [58]. This dataset is referred to in the present work as the Homer dataset. The Homer dataset contains GB structures that have 150 different CSL values corresponding to unique disorientations up to Σ 999, sampled at intervals of ~ 5° in the disorientation space. For each CSL value, a sampling of boundary planes was selected to provide comprehensive coverage, making 7304 unique GBs in the 5D space of GB crystallographic character.² The optimal atomic configuration for each GB was then found by varying 6 parameters of GB construction while maintaining the 5D constraint of the GB, relaxing each structure via conjugate gradient energy minimization. In this work we examine only the minimum energy configuration of the 6 GB construction parameters. See [52] for additional details about the construction of the Homer dataset.

Segregation energy values in Eq. (1) were computed in LAMMPS molecular statics simulations [59] using the Ni-Al-Co empirical EAM potential from Purja Pun et al. [60], which is the same potential used by Huber et al. [31] and Wagih et al. [27]. Note that Co is known to develop a magnetic moment [61], but this EAM potential has been carefully fitted to the Al-Co phase diagram [60] and all our calculations are with individual Co atoms. Therefore, we assume that magnetic effects are negligible and can be disregarded in this work. In addition, this potential reproduces similar GB behavior to the Mishin potential [58] used in the creation of the GB dataset. We start with a relaxed GB structure and replace an existing Al atom with a Co atom at the same atom site. The entire GB structure is then relaxed via conjugate gradient minimization to an energy and force tolerance of 10^{-10} relative error and 10^{-10} eV/Å, respectively. Following minimization, the segregation energy for the substituted atom, E_{ceg}^{Coj} , is calculated using Eq. (1). This process was completed for approximately 70 million atoms

This process was completed for approximately 70 million atoms from 7272 GBs: each atom closer than 15 Å to the GB plane was replaced by a Co atom, as well as a random sample of 100 atoms for each GB in the range of 15–25 Å to use for bulk reference energies ($E_{Co}^{ref} \& E_{Al}^{ref}$). Atoms further away from the GB are not substituted because E_{seg}^{coq} rapidly falls to 0 eV with distance from the GB plane [62,63].

2.3. Analysis techniques

Since the segregation data for each GB results in a spectrum of values, we employ multiple methods to simplify comparison of the spectra across the set of GBs. Two methods that require additional description are (i) a classification scheme and (ii) a GB solute concentration, which are described below.

For reasons that will be clear in the verification Section 3.1.1, we implement a classification scheme that classifies any atom with nearbulk segregation behavior as "negligibly segregating." We do this because the segregation energy values of the bulk atoms actually take on a range of values about 0 eV and GB atoms with segregation energy values in that same range would behave the same as if they were in bulk. We designate segregation energy values in the 95% interval³ of the bulk atom distribution as "negligibly segregating." This allows us to more easily determine which atoms are "segregating" and "anti-segregating"

¹ Eq. (1) is an approximation for the free energy or enthalpy change due to the solute segregation at the GB. This formulation is only valid in the dilute limit, since it neglects solute-solute interactions [57].

 $^{^2\,}$ 10 of the 7304 GB structures in the Homer dataset [53] are excluded from this work due to computational difficulties. See Supplemental Table S3 for a list of excluded GBs.

³ Supplemental Figure S3 shows a number of intervals on the distribution of FCC atoms, from which we selected the 95% interval for the "negligible" classification. Supplemental Figure S4 shows a number of intervals on the distribution of non-FCC atoms.

because they are outside the range of typical bulk atom segregation energies. The ranges for these three possible classifications are: (i) segregating; $E_{\text{seg}}^{\text{Co}_l} < -0.0875 \text{ eV}$, (ii) negligibly segregating; $-0.0875 \text{ eV} \le E_{\text{seg}}^{\text{Co}_l} < +0.018 \text{ eV}$, and (iii) anti-segregating; $E_{\text{seg}}^{\text{Co}_l} \ge +0.018 \text{ eV}$. A standard measure of solute segregation at GBs is the solute con-

A standard measure of solute segregation at GBs is the solute concentration at the GB in the dilute limit, c_{GB} . Early literature calculated this value using a single effective segregation energy [14] or a continuous distribution of segregation energies for atoms in the GB [64]. This type of approach is computationally simple but has some pitfalls (as mentioned in Section 1) that can be avoided by using a discrete segregation energy spectrum. Coghlan and White first created such a spectrum [22], which was later adapted by Huber et al. [31] for an array of individually described atoms in a single GB. The concentration of solute atoms in the GB is then calculated according to:

$$c_{\rm GB} = \frac{1}{N} \sum_{i} \left[1 + \frac{1 - c_{\rm bulk}}{c_{\rm bulk}} \exp\left(E_{\rm seg}^{\rm Co_i}/k_{\rm B}T\right) \right]^{-1}$$
(2)

where $E_{seg}^{Co_i}$ is defined by Eq. (1), *N* is the number of sites in the GB, k_B is the Boltzmann constant, *T* is the temperature, and c_{bulk} is the concentration of solute in bulk, held fixed as an independent variable. Bulk atom sites are chosen for solute occupancy at finite temperatures with increasing probability, lowering c_{GB} ; the temperature dependence of this value is demonstrated for this work in Section 4, and is a well known feature of GB segregation [65]. The $\frac{1-c_{bulk}}{c_{pulk}}$ term scales the Fermi level down as bulk atom sites are filled at finite temperatures, as discussed in [31]. In this work we use a bulk concentration of $c_{bulk} = 0.2$ at.%, chosen to be the same as in Huber et al. [31].

3. Verification & validation

An important step in collection of any data is the verification and validation of the results [66]. In the following sections we verify that the calculated values are representative of true segregation energies and validate the results by comparing them to other published examples.

3.1. Verification

In verifying the data collected in this work, we noted that some data was incorrect or did not match expected behavior. The following sections discuss the process of determining which data could be verified for accuracy and inclusion in the work.

3.1.1. Verification of bulk segregation energies

By definition (Eq. (1)), solute atoms in the bulk have segregation energies of 0 eV. In order to verify this behavior, we must classify atoms as either bulk or GB atoms. The method by which the GB atoms are separated from the bulk atoms will have an impact on whether bulk atoms exhibit the expected 0 eV segregation energy. Since a segregation energy spectrum typically only includes GB atoms, the classification scheme can also affect the segregation energy spectra based on the inclusion of atoms near or in the GB that may or may not have segregation energies near 0 eV.

Bulk atoms are often identified in simulations by adaptive common neighbor analysis (aCNA), as employed in [26–28,30–33], which can identify each atom's environment as HCP, BCC, ICO, FCC or other [67]. Alternatively, the centrosymmetry parameter (CSP) [68] can be used to identify atom environments where the expected centrosymmetry breaks down, such as near a GB in an FCC-type crystal structure. One could also identify GB atoms that are within some fixed width (e.g. ± 5 Å) of the center of the GB. There are several other less commonly used methods to determine bulk atoms, such as the dislocation extraction algorithm (DXA) [69,70] used in [42], the per-site Voronoi volume criterion used in [35], and the experimentally determined one-atomic layer region from the GB center [71,72], as employed in [29].

There are challenges with using aCNA, CSP, and DXA as classification methods because they were designed for purposes other than determining whether an atom belongs to a GB. The aCNA method excels at structure identification, but tolerates distortions of atoms in those structures. The CSP method, since it is continuous, is better suited to differentiate smaller distortions. However, it has no defined cutoff value for discerning when a distortion has changed the structure sufficiently to be classified as something other than the centrosymmetric structure of interest (FCC in this case); this is left for the user to choose. The fixed width method does not generalize easily to polycrystal simulations, and due to relaxation in the positions of atoms near the initial position of the GB plane, defining the center of the GB can be difficult, especially in the case of GB faceting. Additionally, the width of the GBs across a single dataset can very drastically (e.g. Fig. 5 in ref [52] shows that the width of GBs in the Homer dataset range from 3-18 Å, and the selection of a single fixed width would bias the number of FCC atoms included). Since other methods suffer from similar challenges, there is no clear way to determine whether an atom definitively belongs to the GB because the transition from bulk to GB can be subtle; elastic strains that cause small deviation from a "perfect" bulk structure are present even at large distances.

These challenges and the differences between the most commonly used methods of aCNA and CSP classification are illustrated in Fig. 1 for (a) a [100] symmetric tilt GB with an array of edge dislocations and for (b) a high-angle GB. The atoms are colored according to their segregation energy value (red for anti-segregating, blue for segregating, gray for negligible). The figure depicts the full structure of the GB in the "All atoms" row and the three below that depict the use of progressively smaller CSP threshold value to remove "bulk" atoms. The "CNA" row shows that the aCNA is aggressive in its removal of "bulk" atoms, since its goal is not to identify local distortions in structure but clear changes in crystal structure. The result is that many surrounding atoms with non-negligible segregation energy values are removed by aCNA bulk determination.

Fig. 1 illustrates that there is no definitive approach to atom selection for 0 eV bulk GB segregation energies using aCNA or CSP. In this work, we present results for bulk atom selection using both aCNA and CSP methods to compare the impact the selection method has since the aCNA method removes many atoms that could meaningfully contribute to segregation energy spectra. We also show cumulative segregation energy spectra of several fixed width cutoffs in Supplemental Figures S5 and S6, where liberal width leads to CSP-like distributions and conservative width leads to aCNA-like distributions. In this work, CSP labeled results use a CSP cutoff of 0.1, as it includes a reasonable number of surrounding atoms with non-negligible values of the segregation energies while limiting the number of bulk atoms with negligible values of the segregation energy.

Supplemental Section S1 contains a discussion comparing bulk atom selection by the aCNA and CSP techniques. The discussion can be summarized in the segregation energy distributions of the bulk atoms by the two classification techniques shown in Fig. 2. The majority of bulk atoms have segregation energy values close to 0 eV, though there is a larger than expected variation in the local environments of bulk atoms as determined by both aCNA and CSP. In short, both bulk atom classification schemes classify some atoms as bulk even though they have non-negligible segregation energy values. Given the range of elastic strains near defects, it remains a challenge to find a single defensible method to identify GB and bulk atoms. By contrasting the aCNA and CSP bulk classification schemes in this work, we illustrate the difference between conservative and liberal classification schemes. The determination of a better method for selecting GB atoms is left for the community to resolve.

Recalling that theory defines segregation energy of an atom in the bulk as equal to 0 eV, one would expect segregation energies to converge to 0 eV as distance from the GB plane increases [62,63]. In



Fig. 1. Atomic structures of (a) a [100] symmetric tilt GB with an array of edge dislocations and (b) a high angle, low symmetry GB. Both GBs are shown with "All atoms", "CSP" bulk atom removal (2nd row: CSP ≤ 0.3 , 3rd row: CSP ≤ 0.1 , 4th row: CSP ≤ 0.01), and adaptive "CNA" bulk atom removal. Red atoms have positive segregation energies, blue have negative, and gray have negligible, according to the colorbar shown. In both cases, the positive *y*-axis corresponds to the positive *z*-axis in the GB simulations, and the GB plane is located at z = 0 Å. The crystallographic directions for each are given in Supplemental Table S2. The GB images are produced using OVITO [73]. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)



Fig. 2. Logarithmic scale of the distribution of segregation energies for bulk atoms as determined by CSP \leq 0.1 (blue) and aCNA (orange). Bin width is 0.008 eV. The aCNA peak is broader because it classifies more distorted atoms as bulk. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

an initial analysis, it was found that while the majority of data behaved in this way, some did not converge to 0 eV more than 15 Å away



Fig. 3. (Top) Histograms of segregation energy for GB atoms (blue), bulk atoms (gray), and atoms in GBs excluded due to invalid calculations (red). Bin width is 0.165 eV. A linear-scale histogram with the same data is included as Supplemental Figure S8 to show how low segregation energies contribute negligibly to the distribution. (Bottom) Distance from the GB plane in Å as a function of segregation energy, (E_{seg}^{Co}) . In the GB construction simulations, the GB plane is initialized at z = 0 Å and is allowed to shift as the simulation cell relaxes, however, this distance is calculated as a distance from z = 0 Å. The non-converged and low energy GBs that were removed from analysis as described in Sections 3.1.1 and 3.1.2 are shown in red, the bulk FCC atoms as determined by a CSP cutoff of 0.1 are shown in gray, and the non-bulk GB atoms are shown in blue. The distribution decays to 0 eV as the distance from the GB increases (with the exception of the references to color in this figure legend, the reader is referred to the web version of this article.)

from the GB plane. This is illustrated in a scatter plot of segregation energy vs. distance from the GB plane in Fig. 3 for three different populations. These populations make up the 70 million atoms and are: the bulk atoms (gray), the GB atoms (blue), and atoms belonging to GBs excluded from the dataset because of errors described here and the following section (red). Four GBs in particular account for the scatter (non-zero segregation energy values) at large distance from the GB, and were therefore excluded from further analysis. These four GBs are listed in Supplemental Table S3 along with GBs excluded for reasons that are discussed in the next section. It can be seen in Fig. 3 that there are still GB atoms at large distance from the GB, but in all cases these have segregation energy values near zero; furthermore, there are very few of these, so they contribute negligibly to the spectra of individual GBs.

3.1.2. Challenges due to GB restructuring

There are a small number of very negative segregation energy values, far below what would be expected for this system, which are illustrated by the red data points in Fig. 3. When substituting a solute atom for segregation energy calculations, the energy of the new system is calculated after the system has relaxed into the new configuration that accommodates the solute atom. Usually, this relaxation results in almost no change to the atom positions. However, non-negligible changes to the atom positions occasionally occur. The reference energy $E_{\rm Al}^i$ (in Eq. (1)) pertains to the original pre-substitution configuration and not the restructured configuration, therefore the segregation energy values are not valid when significant restructuring occurs. A valid segregation energy value for the restructured configuration would require calculation of a new reference energy, $E_{\rm Al}^i$.

To determine when GB restructuring occurs and the magnitude of such restructuring, we calculated the mean squared displacement (MSD) for all atoms in a GB during the relaxation following solute substitution. Generally, the MSD at GB atom sites was found to be higher than the MSD at FCC bulk atoms (see Supplemental Figure S7), but there is considerable overlap between the two distributions. A plot of segregation energy vs. MSD is shown in Supplemental Figure S9. In this figure it can be seen that (i) the most extreme segregation energies occur when the MSD values are higher and (ii) there are also lots of reasonable segregation energies with relatively large MSD values. Here, we examine examples of these two cases.

In one case where the segregation energy was very negative, $E_{seg}^{Co_i} = -6.1$ eV, and the MSD value was large, 0.076 Å², considerable restructuring occurred during the post-substitution relaxation. To check the accuracy of this atom's segregation energy value, new reference energy values were determined using the restructured GB for the reference energies. The segregation energy value was re-calculated to be $E_{seg}^{Co_i} = -0.45$ eV. Restructuring clearly caused the reference energies to be invalid for the post-substitution GB structure in this case, and MSD was a good determination of this invalidity.

In another case where the segregation energy was in the normal range, $E_{\rm seg}^{\rm Co_i} = -0.38$ eV, but the MSD was still reasonably large, 3×10^{-4} Å², there was minimal restructuring. The accuracy of this atom's segregation energy value was also checked, and even with new reference energy values, the segregation energy value remained the same at $E_{\rm seg}^{\rm Co_i} = -0.38$ eV. In this case, the atomic shuffles had no impact on the segregation energy and the larger than expected MSD values were not indicative of invalid segregation energy values.

Although some high MSD value simulations yield valid segregation energies, we attempted to address the issue of invalid segregation energies caused by restructuring by omitting atoms where MSD values were large. We defined a high-MSD cutoff of 10^{-4} Å², since it was above this MSD value that the low segregation energies started to diverge (cf. Supplemental Figure S9). Unfortunately, this approach removed 7 entire GBs and 38% of the atoms from analysis. Additionally, in some individual GBs, most of the data was lost, as illustrated in Supplemental Figure S10, which shows the effect of removing atoms with high MSD values. This approach also removed segregation energy values that were valid, as indicated by the second case examined above. This approach causes severe data loss and could lead to misinterpretations of the results.

Additional analysis showed that most of the extreme (and likely invalid) segregation energy values belonged to a small number of GBs, and these GBs had a high percentage of extreme segregation energy values. In other words, certain GBs were prone to restructuring upon substitution of a solute atom. While not a perfect solution, we removed 18 GBs with segregation energy data less than -3.0 eV, which belong to the population of atoms in the excluded GBs shown in red in Fig. 3 and listed in Supplemental Table S3. Supplemental Figure S11 shows the segregation energy spectra for other possible segregation energy cutoff values. The chosen cutoff value of -3.0 eV removes most of the extreme values while only removing 0.25% of the GBs simulated.

While this approach leaves some invalid data in the spectrum due to restructuring in individual simulations, the removal of these 18 GBs seemed the best option, as it only removes 0.25% of the GBs. We assume that the contributions of any remaining invalid datapoints to the spectrum is minimal, as illustrated in Fig. 3. One way to get around this issue in the future would be to recalculate the reference energy

values any time restructuring is detected. Unfortunately, recalculating these reference energies after the fact was impractical for this work.

3.1.3. Final dataset

As discussed in Section 3.1.1, 4 GBs were removed due to the failure to converge to a zero segregation energy value in the bulk. Another 18 GBs were removed from the dataset because they possessed extremely low segregation energy values, as discussed in Section 3.1.2. There were 10 GBs that were not included due to issues refilling the partially full simulation cells in the dataset. These 32 GBs are listed in Supplemental Table S3. The remaining data contains 70 million atoms with segregation energy values to analyze from 7272 unique GBs. With bulk atoms removed via CSP or aCNA, this number is reduced to 18 or 11.5 million GB atoms, respectively. Despite the imperfections of these methods as discussed above, it is anticipated that this dataset will provide unique insight into segregation energy trends and is available for download [74]. Having verified the Homer dataset here, we validate it in the following section.

3.2. Validation

In order to validate our work, we compare our results to two computational datasets of Co segregation energies in Al GBs that use the same EAM potential [60] and similar methods to this work; no experimental data for Co enrichment in an Al matrix could be found. Huber et al. examine a number of Σ 5 GBs in [31], and Wagih et al. examine a polycrystal with a variety of different GBs and focus on the overall distribution of segregation energies in [27]. These two datasets are referred to as the Huber dataset and Wagih dataset in the following sections where they are compared with the present results obtained from the Homer dataset.

3.2.1. Comparison to selected $\Sigma 5$ GBs

Huber et al. examine solute segregation in a GB dataset of 38 Σ 5(53.1°[100]) GBs [31]. The Homer dataset includes 17 GBs of this type, although the two datasets only have four GBs that share all 5 crystallographic degrees of freedom. Fig. 4 compares the segregation energy spectra for these four GBs. Fig. 4a is from the Huber dataset with a kernel density estimation (KDE) fit shown with a solid line and a model fit described in [31] shown with a dashed line. Fig. 4b is from the present work using the Homer dataset, with segregation energies for non-bulk atoms as determined by aCNA, which is the same method used by Huber et al. [31]. Fig. 4c is also from the present work using the Homer dataset, but with segregation energies for non-bulk atoms determined by CSP. KDE fits to the distributions in (b) and (c) are shown with solid lines.

The locations of segregation energy peaks and their relative magnitudes are similar. The $[0\bar{2}1]$ GB has the most favorable comparison, though the Huber dataset in (a) has a small scattering of infrequent peaks that do not show up in the aCNA Homer dataset in (b). In (c), the CSP Homer dataset has an additional peak at approximately -0.05 eV. The $[0\bar{1}2]$ GB has peaks in the same general locations, but slightly different relative magnitudes, again with more scatter in the peaks of the Huber dataset. The CSP Homer dataset again has a large population of atoms with segregation energies near -0.10 eV and an additional peak near 0.10 eV in both (b) and (c). The [100] GB in our work has a missing peak at approximately -0.55 eV, and an additional missing peak near -0.01 eV in (b) that is present in (c). Finally, the $[1\bar{1}2]$ GB has more distinct peaks in (b) and (c) that make up the multimodal distributions around -0.50 eV, 0.00 eV, and 0.30 eV in (a), and a higher relative magnitude in the peak near 0.00 eV.

In all of the GBs, (c) seems to have more data around -0.05 eV, indicating that bulk determination via CSP leaves a larger population of atoms with near-negligible segregation energies. These same atoms are removed by the aCNA bulk determination method, which may explain why aCNA is used in many other works for bulk classification.



Fig. 4. Segregation energy distributions of the shared $\Sigma 5$ GBs between the (a) Huber dataset from [31] (bin width 0.04 eV) and the (b/c) Homer dataset (bin width 0.01 eV). (a) has two fit lines: a KDE fit to the data (solid) and a model fit discussed in [31] (dashed). (b) includes the non-bulk atoms from this work as determined by aCNA (the same method of FCC atom removal as is used in [31]). (c) includes the non-bulk atoms from this work as determined by CSP. The Huber dataset in (a) is reproduced from [31] and relabeled according to the Homer dataset labeling conventions [52,53].

However, it can be noted that these values are not identically zero, and contribute to the overall relative frequency of the various peaks. This observation is not to advocate for one method over another, but simply to acknowledge a bias introduced by the method of bulk and GB atom selection.

The segregation energy spectra of the two datasets are in general agreement, with appropriate magnitudes and frequency of occurrence. Clearly there is not an exact match, perhaps due to the GBs not having identical structures or not extracting the same GB atoms. For example, the high symmetry structure of the $\Sigma 5$ GBs in column 1 of Fig. 4 has only 6 GB sites as determined by CNA. Any small variations in GB structure and/or GB atom selection could result in the addition or subtraction of a GB atom, which would lead to large changes in the spectra by adding or subtracting entire peaks. For example, the missing peak at approximately -0.55 eV in the [100] GB from the Homer dataset when using both aCNA and CSP indicates that the local atomic environment making up that peak in the Huber dataset is not found in the Homer dataset. With no atomic structures from the Huber dataset published, we are unable to verify this conclusion. However, given the fact that we cannot guarantee identical atomic structures, we consider the general agreement of the segregation energy spectra to be sufficient validation of the Homer dataset in comparison with the Huber dataset.

3.2.2. Comparison to polycrystal spectrum

While the Homer dataset contains only bicrystal GBs, most materials are polycrystalline, containing a GB network with additional features such as triple junctions and facets. Some recent works have focused on extracting segregation energy distributions from polycrystalline simulations [26–29,50,51]. Here we compare the spectrum of segregation energies obtained from bicrystals of the present work with that obtained by Wagih et al. from a polycrystal [27]. The Al-Co segregation energy spectrum from the Wagih dataset is represented by a skew-normal distribution of the form:

$$F(E_{\text{seg}}^{\text{Co}_i}) = \frac{1}{\sqrt{2\pi\sigma}} \exp\left[-\frac{\left(E_{\text{seg}}^{\text{Co}_i} - \mu\right)^2}{2\sigma^2}\right] \operatorname{erfc}\left[-\frac{\alpha\left(E_{\text{seg}}^{\text{Co}_i} - \mu\right)}{\sqrt{2\sigma}}\right]$$
(3)

with the fitted location parameter μ , scale parameter σ , and shape parameter α . Note that these values are not the typical mean, standard deviation, and shape parameter of a normal distribution.⁴

The segregation energy spectra for this work are presented in Fig. 5. The spectra from the Homer dataset are obtained by combining the individual GB segregation energy spectra from all 7272 GBs. There are two distributions for the two methods by which bulk atoms are removed: aCNA in blue and CSP in orange. The figure includes the Wagih spectrum, scaled to match the two distributions in this work, plotted as dashed black lines, and skew-normal fits in solid lines in corresponding colors to the spectra. Note that the authors use a skew-normal form for the sake of comparison, and did not attempt to find another functional form with a better fit. See Supplemental Figures S5 and S6 for the spectra created using fixed width bulk determination.

First, we note that the inclusion of bulk-like atoms using the CSP approach leads to a much larger peak near the origin, though other parts of the histogram of segregation energies are very similar between the aCNA and CSP distributions of the Homer dataset. A comparison of statistical measures of the distributions, in the form of Eq. (3), are provided in Table 1. It can be seen from Table 1 that the aCNA and CSP distributions of the Homer dataset are in general agreement.

To compare the current data to the Wagih dataset, we scaled the magnitude of the skew-normal distribution fitted to the Wagih dataset to match the magnitude of both distributions of the Homer dataset. Note that the Wagih dataset uses aCNA for bulk classification. Despite

⁴ Others have also observed the skew-normal form of the spectrum of segregation energies in GBs, including when bicrystals are used [75,76].



Fig. 5. The spectrum of segregation energies aggregated from all GBs simulated in this work, with all bulk atoms removed via aCNA (blue) and via CSP (orange), with fit lines for their respective skew-normal distributions in the form of Eq. (3) in their respective colors. The dashed black lines are the polycrystal spectrum from Wagih et al. in [27], scaled to both of this work's distributions. Inset are the same spectra on a logarithmic scale. Statistics for each skew-normal distribution are given in Table 1. The spectrum of all atoms (including bulk atoms) is shown in Supplemental Figure S12. Bin width is 0.0412 eV. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

Table 1

Comparison of skew-normal statistical measures for the distributions shown in Fig. 5. These parameters—the fitted location parameter μ , scale parameter σ , and shape parameter α —are for the skew-normal distribution described in Eq. (3). Note that these are not the usual mean, standard deviation, or shape parameter of a Gaussian distribution. Fixed width distributions are shown in Supplemental Figure S5 and Supplemental Table S1.

Dataset	μ	σ	α
Polycrystal [27]	-0.0104	0.3224	-3.300
Bicrystals, no FCC via aCNA	0.0328	0.3794	-2.424
Bicrystals, no FCC via CSP	0.0706	0.3502	-3.365

their quantitative and statistical similarity, there are notable differences in the bicrystal and polycrystal spectra. In comparison to the polycrystal spectrum, the bicrystal spectra have a slightly higher number of sites with segregation energies just greater than zero and a slightly lower number of sites with segregation energies just less than zero. In the inset with the frequency on a logarithmic scale, it can be seen that there is also significant divergence of both bicrystal spectra from the polycrystal spectrum in the lower tail, but this difference is negligible in the linear frequency scale.

The source of the differences in the two spectra is likely due to the differences in the datasets. First, the polycrystal dataset has 16 distinct grains, 72 GBs, and ~ 10^5 non-bulk GB atoms [27], in comparison to the 2×7272 distinct grains, 7272 GBs, and ~ 10^6 non-bulk GB atoms for the bicrystals in the present work. In addition, the polycrystalline simulation has atomic environments found in GB triple junctions and quadruple nodes that may not appear in bicrystal simulations, or if those environments show up in bicrystal GB simulations, they may appear with a different frequency than they do in a polycrystalline structure.

It has been shown that small populations of bicrystal GBs fail to produce the same segregation energy distributions as those of polycrystalline materials [50,51], but that as the population diversity increases with GBs of lower symmetry, there is better coverage of the atomic environment space [51]. The present dataset of 7272 bicrystal GBs is comprised of mostly low symmetry GBs; only 89 of the 7272 GBs, or 1.2%, have low CSL values (i.e., $\Sigma \le 10$), suggesting that issues related to diversity in the dataset are minimized by the large variety of GBs in the Homer dataset.

Conversely, the polycrystal simulation with its 72 GBs may not provide adequate sampling of the variation in structure across the 5D space, or be large enough to be considered a representative volume element (RVE) such that it is truly representative of atomic environments in a polycrystal. The Mackenzie Distribution, which represents the distribution of disorientation angles for a polycrystalline sample with random cubic crystal orientations [77,78], can be used as a justification for the selection of an RVE [79]. As shown in Figure 3 of [52], the Homer bicrystal dataset gives a reasonable approximation of the Mackenzie Distribution. The Wagih polycrystal dataset does not claim to follow the Mackenzie Distribution of disorientations, nor do they consider their simulation to be an RVE. Wagih et al. do however assert that their simulations are similar enough to randomly oriented grains to represent the local atomic environments present in the polycrystalline GB space, and that the segregation energy spectrum obtained is universal to any segregation energy spectrum obtained from a polycrystal [26,51].

At this point, it is unclear if the differences between the Wagih and aCNA bicrystal distributions are significant. The degree to which either of the methods incorporates aspects of the distribution of GBs that are critical to a proper representation of segregation energies in a diverse polycrystal is also unclear. The discussion leads to several unanswered questions:

- 1. How many GB types would be needed to establish an RVE for segregation energies? (i.e., is the polycrystal sample from Wagih et al. large enough? Does the present work have enough and sufficiently diverse bicrystals to represent a polycrystal?)
- 2. How would a change in GB texture of the polycrystal change the GB sampling and thus the segregation energy spectrum? (i.e., does the texture used in the work of Wagih et al. bias the sampled spectrum significantly? Is it appropriate to make these distributions from a random sampling?)
- 3. To what degree do the local atomic environments of triple junctions and quadruple nodes affect the sampled segregation energy spectrum? (i.e., the volume fraction of such atomic environments will be different in nanometer-sized grains as compared with micron-sized grains, and may be entirely absent from the bicrystal dataset of this work.)

We leave these questions to the community to address. Nevertheless, the similarity in the two spectra is seen as a positive validation of the methods and use of the Homer GB dataset in this work.

4. Results & discussion

Having provided some context and discussion of the results in the Verification & Validation section, we begin our analysis here by taking several different views of the segregation energy spectra produced in this work. Note that most of the results presented in this section are produced using CSP to determine bulk atoms, but similar results would be obtained using aCNA, as shown in the supplemental materials and described in Section 4.4.

Examining the spectra of segregation energies across the 5D space is challenging because at each point in the space we obtain a spectrum of segregation energies. To provide insight into the dataset, we employ several different tactics: (i) statistical measures of the spectra, (ii) classification of the segregation energy spectra into fractions of atoms segregating, anti-segregating, and negligibly segregating, and (iii) calculation of a GB solute concentration for each GB ($c_{\rm GB}$ defined in Eq. (2)) based on Coghlan and White's model [22]. Each of these provide different insight into trends in the large set of GBs. Table 2

Statistics for the $\Sigma 5$ GBs shown in Fig. 4. Note that the max, mean, and min values in the table refer to the maximum, mean, and minimum values from each GB's $E_{seg}^{Co_1}$ spectrum.

GB	max (eV)	mean (eV)	min (eV)	$f_{\rm seg}$	$f_{\rm negl}$	$f_{\rm anti}$	c _{GB} (at.%)	$\gamma \left(\frac{mJ}{m^2}\right)$	$V_{\rm exc} \left(\frac{\mathring{A}^3}{\mathring{A}^2}\right)$
021	0.52	-0.01	-0.31	0.29	0.29	0.43	28.9	494	0.529
012	0.46	-0.14	-0.53	0.47	0.40	0.14	37.7	496	0.347
100	0.34	-0.05	-0.20	0.44	0.44	0.11	35.5	326	0.296
112	0.30	-0.18	-0.57	0.58	0.24	0.18	59.7	472	0.340



Fig. 6. Maximum (red), mean (green), and minimum (blue) values of the segregation energy, E_{xeg}^{Co} , spectrum for each GB vs. their GB interface energy, γ . Linear fits for each are shown in black. The mean segregation energy for the [111] symmetric twist GBs are shown with black "x" markings. The range of segregation energies increases with GB energy, and the mean segregation energy has an inverse relationship with increasing GB energy. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

4.1. Statistical measures of the spectra

In this section, to examine the segregation energy spectra across all of the dataset, we present the mean, maximum, and minimum values of the multimodal distributions of each GB's segregation energy spectrum. As an example, the maximum, mean, and minimum values for the $\Sigma 5$ GB spectra shown in Fig. 4c are given in Table 2.

Although this represents a significant reduction of information, some observations can be still made by comparing these values against one-dimensional parameterizations of the GB dataset. For example, these values are plotted as a function of GB interface energy, γ , in Fig. 6 and disorientation angle in Supplemental Figure S13. Generally, the mean segregation energy of a GB becomes more negative as GB energy increases, as shown by the green datapoints and trendline in Fig. 6. Note that the [111] symmetric twist GBs (aside from the lowest energy perfect twin GB) have a slight increase of the mean segregation energy as GB energy increases, contrary to the general trend. We will further analyze this subset of GBs in Section 4.3 because of their likely presence in Al [80]. The average range of segregation energies also increases as a function of GB energy, as indicated by the linear fits to the three populations shown in black. This is probably due to greater deviation from the bulk FCC structure in the higher energy GBs, which likely leads to a greater distribution of segregation energies in the solute atom sites. Finally, it can be seen in Fig. 6 that the lower the mean segregation energy for a GB, the higher the probability for segregation in that GB.

GB energy, γ , has been shown to have a Read-Shockley relationship with disorientation angle [81,82]. Despite the relationship observed between GB energy and mean segregation energy, there is no observable transitive relationship between mean segregation energy and disorientation angle (see Supplemental Figure S13). It is interesting that the two separate correlations do not result in a correlation between segregation energy and disorientation angle. While the correlation of segregation energy with GB energy provides some insight to global trends in segregation energy, we continue with more detailed analyses of the dataset.

4.2. Classification of the spectra

To examine the segregation energy spectra in this section, we employ the segregation energy classifications described in Section 2.3. This approach classifies each atom based on its segregation energy value into one of three categories: (i) segregating ($E_{seg}^{Co_i} < -0.0875 \text{ eV}$), (ii) negligibly segregating ($-0.0875 \text{ eV} \le E_{seg}^{Co_i} < +0.018 \text{ eV}$), or (iii) anti-segregating ($E_{seg}^{Co_i} \ge +0.018 \text{ eV}$). Using these classifications, we compute the fraction of atoms in each GB that fall into each category, (i) f_{seg} , (ii) f_{negl} , and (iii) f_{anti} . For each GB, these fractions add to 1 (i.e., $f_{seg} + f_{negl} + f_{anti} = 1$). As an example, the f_{seg} , f_{negl} , and f_{anti} values for the $\Sigma 5$ GB spectra shown in Fig. 4c are given in Table 2.

The distributions of these fractions for the 7272 GBs are shown in Fig. 7a; these are the distributions for non-bulk atoms identified using the CSP scheme. The mean value for these categories over all GBs are $\overline{f_{\rm seg}} = 0.62$, $\overline{f_{\rm anti}} = 0.15$, and $\overline{f_{\rm negl}} = 0.23$, as shown by the dotted vertical lines in Fig. 7a. The global fractions in the aggregated spectrum are $f_{\rm seg} = 0.63$, $f_{\rm anti} = 0.15$, and $f_{\rm negl} = 0.22$.

In Fig. 7b, this same data is shown on a ternary plot, that shows the 2D plane that the 3D points all lie on, since they all add to 1 (i.e., $f_{seg} + f_{negl} + f_{anti} = 1$). The data points in the plot are colored by GB energy, γ . It can be seen in Fig. 7b that increased GB energy corresponds to an increased fraction of segregating atoms, f_{seg} . This supports the trend for more negative segregation energies with higher GB energy observed in Fig. 6. To see the same plots for aCNA, see Supplemental Figure S14.

As expected from the histograms, the general distribution of points in Fig. 7b is located closest to the "all segregating" corner of the triangle. There are several notable outliers. The [111] perfect twin GB is located at "all anti-segregating" and its closest neighbor in the ternary plot has the same misorientation of 60° about the [111] axis. [100], [110] and [111] disorientation axis GBs make up 50% of the GBs along and near the top right edge of the triangle with $f_{negl} \leq 0.1$. 34% of the GBs with $f_{anti} \leq 0.075$ belong to the [111] disorientation axis.⁵ Thus, many of the outliers in the ternary plot belong to high symmetry disorientation axes. Additionally, it can be seen that there are a number of GBs along the left side of the plot which have no anti-segregating atoms, though this is perhaps unsurprising given the proximity of the distribution to this edge and the tendency to segregate in this system.

In short, most GBs have a tendency to segregate, evidenced by the $\overline{f_{seg}}$ value of 0.62. Additionally, high energy GBs have a tendency

⁵ To see the ternary plot with the [111] disorientation axis GBs highlighted, see Supplemental Figure S15.



Fig. 7. (a) Histograms of f_{seg} (blue), f_{anti} (red), f_{negl} (gray) for GB atoms as determined by CSP. The mean of each histogram is marked with a dashed vertical line of a corresponding color. Bin size is 0.005 eV. (b) Ternary scatter plot of the same data, colored by GB energy, γ . Since the sum of these values is 1 (i.e., $f_{seg} + f_{anti} + f_{negl} = 1$), they lie on a 2D plane in 3D space. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

to segregate more than lower energy GBs, which is supported by the results shown in Fig. 6. However, while these trends are interesting, this analysis is still insufficient to predict segregation behavior generally.

4.3. Solute concentration at GBs

One of the challenges with the representations of the segregation energy spectra analyzed in the preceding sections is that they still have multiple values for each GB, which makes it hard to analyze trends across the 5D space. As such, we have included the calculation of the GB solute concentration, $c_{\rm GB}$, from Eq. (2). This singular value for each GB allows the display of some trends more clearly in subsets of the 5D space that still take into account attributes of the full spectrum of GB energies, as the value is computed from a sum over the whole spectrum of GB atoms in each GB. Note that most of the $c_{\rm GB}$ values presented in this section are well above the dilute limit; as such, many of the assumptions made in the calculation of the concentration values (e.g., neglecting solute-solute interactions) are invalid. However, we assume that the general trends observed in $c_{\rm GB}$ are still valid.

As with the other sections, the $c_{\rm GB}$ values for the $\Sigma 5$ GB spectra shown in Fig. 4c are given in Table 2. However, because $c_{\rm GB}$ takes into account the full spectrum, we can more easily examine the impact of the GB crystallographic character on segregation. We do this first in



Fig. 8. (a) Plot of GB energy and GB excess volume as functions of disorientation angle for the [111] symmetric twist GBs. (b) Plot of the segregation energy spectra for GB atoms as determined by CSP (orange) and aCNA (blue) in the [111] symmetric twist GBs, against their disorientation angles. Aside from the perfect twin GB at 60° twist, their segregation energies are almost always negative, or favorable to segregation. The "negligible segregation" ($-0.0875 \text{ eV} \leq E_{\text{seg}}^{C0} < +0.018 \text{ eV}$) limits are shown with dotted black lines. (c) Concentration of solute at the GB, c_{GB} , as a function of disorientation angle and temperature for the [111] symmetric twist GBs, for CSP (solid) and aCNA (dotted). This is calculated using Eq. (2). The bulk concentration, $c_{\text{bulk}} = 0.2 \text{ at.}\%$, is shown with a solid black line. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

the set of [111] symmetric twist GBs noted in [52] and mentioned in Section 4.1 because of their likely appearance in Al due to their low energy [80] and because they show interesting segregation energy results. However, care should be exercised in extrapolating the [111] symmetric twist GB results to the rest of the dataset precisely because they are low energy GBs and may behave differently. Note that the disorientation angles related to these particular boundaries also define their twist angles about the [111] axis. The [111] symmetric twist GBs exhibit an energy trend of an inverted parabola with low GB energy values at low and high disorientation angles, illustrated in blue in Fig. 8a. A corresponding trend for GB excess volume is also shown in orange in Fig. 8a. Fig. 8b plots the segregation energy spectra for the GB atoms as determined by aCNA (blue) and CSP (orange) for each of these GBs, against their disorientation angle. Note the data loss from using aCNA (blue) over CSP (orange), which was discussed in Section 3.1.1. Also note the exclusion of many near-bulk segregation energies in the CSP (orange) spectrum.

Although a significant portion of each GB's spectra falls in the "negligible segregation" category shown by horizontal dotted black lines in Fig. 8b, a majority do not, and almost all of the non-negligible segregation energies are negative, implying that a Co atom added to an Al [111] symmetric twist GB will prefer to segregate to the GB. With the exception of the perfect twin, this segregation data shown in Fig. 8b generally runs counter to the general trend that was observed in Fig. 6 for lower energy GBs to have less segregation energy spectra in Fig. 8b for the corresponding lower GB energies in Fig. 8a, and was perhaps expected from the analysis of the [111] symmetric twist GBs shown with black "x" markings in Fig. 6.

In Fig. 8c, we show the $c_{\rm GB}$ values as determined by CSP (solid) and aCNA (dotted) for the [111] symmetric twist GBs as a function of disorientation angle at 3 different temperatures. In addition to the low energy GBs in this dataset having more negative segregation energies, they also have higher solute concentrations, excepting the perfect twin at 60°. This is seen most clearly in the $c_{\rm GB}$ line for 300 K (orange) in Fig. 8c. This correlation is expected from the inverse relationship between segregation energy, $E_{\rm seg}^{Co_i}$, and solute concentration, $c_{\rm GB}$, in Eq. (2), and can be seen clearly by the paraboloid quality of the segregation energy spectra across disorientation angles in Fig. 8b with a matching inverse paraboloid in Fig. 8c.

As demonstrated in Fig. 8c and expected from Eq. (2), the concentration of solute at the GB, $c_{\rm GB}$, is temperature dependent. Note that segregation energies were calculated at 0 K, but that Eq. (2) expects this to be the case. We expect that as the temperature increases, less favorable atom sites in the bulk of the material are occupied with increasing probability. This causes the concentration to approach the bulk value of $c_{\rm bulk} = 0.2$ at.% at elevated temperatures, which is shown clearly by the decreasing concentration values at higher temperatures in Fig. 8c. Thus the concentrations calculated here match the theory presented in Section 2.3.

The perfect twin GB at a 60° twist angle about the [111] disorientation axis is an exception to most of the trends in the [111] symmetric twist GBs discussed here. For example, it has all positive segregation energies, shown in Fig. 8b. This is unsurprising given the structure of the twin boundary; its density and structure provide no easy sites for segregation as compared with the bulk (evidenced by its low excess volume), leading to positive segregation energy values in all cases. The highly symmetric structure also results in a very low GB energy, shown in Fig. 8a. The perfect twin has lower $c_{\rm GB}$ values than the rest of the [111] symmetric twist GBs at every temperature, as shown in Fig. 8c, as a result of its entirely positive segregation energy spectrum. It is also the only GB in the Homer dataset with a $c_{\rm GB}$ value below $c_{\rm bulk} = 0.2$ at.%, having a value of $c_{\rm GB} = 0.03$ at.% for T = 300 K.

It can be seen that aCNA and CSP give similar results at 300 K (compare the 300 K solid and dotted lines in Fig. 8c). This was found to be the case for the entire dataset; the correlation between $c_{\rm GB}$ computed from CSP vs. aCNA GB atoms is plotted in Supplemental Figure S16. Using CSP nearly always results in a similar, but slightly lower, $c_{\rm GB}$ value since it includes more near-bulk atoms than aCNA, but the positive correlation means that all trends should remain the same. This similarity in $c_{\rm GB}$ emerges despite the differences in the distributions shown in Fig. 8(b), though it is difficult to point to specific

Table 3

Disorientation axes with the highest mean $c_{\rm GB}$ values, and the number of GBs that belong to that axis.

Disorientation axis	$\overline{c_{\mathrm{GB}}}$ for this axis	# of GBs
[443]	52.7 ± 4.6 at.%	86
[751]	51.4 ± 5.5 at.%	108
[654]	51.3 ± 7.7 at.%	20

Table 4

Disorientation axes with the lowest mean $c_{\rm GB}$ values, and the number of GBs that belong to that axis.

Disorientation axis	$\overline{c_{\rm GB}}$ for this axis	# of GBs
[100]	40.6 ± 6.7 at.%	217
[554]	41.1 ± 8.5 at.%	32
[110]	42.6 ± 10.4 at.%	352
[111]	$43.0 \pm 11.6 \text{ at.\%}$	253

aspects of the distributions that lead to bigger differences in $c_{\rm GB}$ based on CSP and aCNA for some GBs than others.

Having examined the [111] symmetric twist GBs, we now turn our attention to the $c_{\rm GB}$ values for all 7272 GBs over the 5D space. 82.1% of non-FCC GB atom sites observed in this work, as determined by CSP, have negative segregation energies, which corresponds to segregation being favorable. Therefore, a majority of GB sites will accommodate a Co atom in the dilute limit. This implies that the concentration of Co atoms in the GB, $c_{\rm GB}$, will be higher than in bulk value of $c_{\rm bulk} = 0.2$ at.%, and is evidenced by the mean concentration of all GBs in the Homer dataset, which is $\overline{c_{\rm GB}} = 46.7 \pm 7.2$ at.% at T = 300 K. Supplemental Figure S17 shows $c_{\rm GB}$ vs. GB energy for all GBs in the Homer dataset. Supplemental Figure S18 shows $c_{\rm GB}$ as a function of disorientation angle.

The disorientation axes with the highest and lowest mean $c_{\rm GB}$ values are given in Tables 3 and 4, respectively. It is worth noting that the low $c_{\rm GB}$ disorientation axes in Table 4 have high symmetry, with the exception of the [554] axis. However, it is also worth noting that the mean $c_{\rm GB}$ for the entire dataset lies within one standard deviation of each of both the low and high concentration disorientation axes' mean values given in Tables 3 and 4, aside from the [443] axis. Thus, there is considerable overlap in the distributions. Additionally some of the axes listed here may not be statistically significant enough to be considered outliers, based on their small populations (e.g., the [654] axis containing only 20 GBs). So, while they may have more extreme $c_{\rm GB}$ values in general and also contain some of the GBs with outlying ternary plot locations mentioned in Section 4.2, the actual range of $c_{\rm GB}$ values in all cases is not large and it is difficult to find meaningful trends among the averaged values of the disorientation axes.

The effect of disorientation is shown in Supplemental Figure S20, where the mean concentrations of all of the Homer dataset GBs at each CSL are plotted in Rodriguez space.⁶ Consistent with Table 4, the [100], [110], and [111] disorientation axis GBs have the lowest $\overline{c_{\rm GB}}$ values per disorientation axis, although the [111] axis has a larger deviation. The smooth variation of $c_{\rm GB}$ in Rodriguez space is an indicator that there may be broader global trends in $c_{\rm GB}$, but because these represent averages of dozens of $c_{\rm GB}$ values for the different boundary planes, any functional would be complex.

The effect of boundary plane is illustrated in Fig. 9, which shows three small subsections of the 5D GB space—the (a) [100], (b) [110], and (c) [111] disorientation axis GBs. Shown are volumetric plots of concentration, c_{GB} , where the *z*-axis defines the disorientation angle

⁶ Rodriguez space is also known as Rodriguez-Frank space and is a fundamental zone where the CSL values of cubic-cubic disorientation GBs are defined. It is a 3D parameterization of disorientation, and as such is often used to aid in visualization of 5D datasets of GBs.



Fig. 9. Disorientation angle vs. boundary plane volumetric plots of concentration in the GB, c_{GB} , with isosurfaces colored by different c_{GB} values for 3 different disorientation axes: (a) [100] (b) [110] (c) [111]. These plots are equivalent to stacking boundary plane fundamental zone plots with the same disorientation axes. The [111] symmetric twist GBs are located along the vertical red line in plot (c), with the perfect twin located at the top, corresponding to the darkest blue contour, and the lowest c_{GB} . (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

and the x- and y-axes define a stereographic projection of the boundary plane normal in boundary plane fundamental zones [83]. The vertices of the plots define high symmetry boundaries; the two vertices that terminate each arc are symmetric tilt boundaries about the disorientation axis and the other vertex defines symmetric twist boundaries about the disorientation axis. The [111] symmetric twist boundaries examined in Fig. 8 correspond to the points along the red line in Fig. 9c.

All three plots in Fig. 9 show smooth but unpredictable variation of the $c_{\rm GB}$ from areas with high $c_{\rm GB}$ to other areas of low $c_{\rm GB}$. We refer to this as a complex or rugged landscape [84]. This means that while $c_{\rm GB}$ varies smoothly, there are many irregular local extrema and a lack of symmetry or global trends. Of the three axes shown in Fig. 9, the [111] disorientation axis in (c) exhibits the largest range of $c_{\rm GB}$. This is perhaps unsurprising because it has the low energy twin GB at the top of the red line, and Table 4 shows that it has a large standard deviation of 11.6 at.%. Additionally, as noted above, GBs from the three axes in Fig. 9 make up many of the outliers in the ternary plot in Fig. 7b, which may be related to their low mean $c_{\rm GB}$ values (noted in Table 4) as compared to the global mean concentration of $\overline{c_{\rm GB}} = 46.7$ at.%. However, as stated earlier, not every GB from these axes will be an outlier.

While there are not broad global trends that we can extract from these few subspaces analyzed, these plots illustrate the effects of disorientation and boundary plane on changes to segregation energy spectra in GBs. The segregation energy spectra or $c_{\rm GB}$ values computed in this work could be used to develop a model for segregation across the 5D space (e.g., using an expansion [85] or an interpolation function [86]). Such a model could subsequently be used to examine the effects of texture or estimate segregation for a GB of arbitrary character.

4.4. Overall trends in dataset

The broad effect of GB crystallographic character on GB segregation trends has to this point been unknown and was recently listed as a future perspective worth considering [48]. The plots of $c_{\rm GB}$ in Fig. 9 and Supplemental Figure S19 show that segregation varies smoothly throughout the 5D crystallographic space. Unfortunately, the landscape produced in this work is rugged and beyond the averaged trends observed in the Rodriguez plot in Supplemental Figure S20, there is no obvious global trend of segregation as a function of 5D crystallographic character. This is futher illustrated in Fig. 10, where the scatter in the data makes it hard to observe any obvious trend between $c_{\rm GB}$ and disorientation angle.



Fig. 10. Disorientation angle vs. concentration in the GB, $c_{\rm GB}$ at 300 K using CSP for GB atom selection. Bin sizes are 0.50° and 0.72 at.%.

This stands in contrast to a variety of experimental reports that show trends of GB enrichment as a function of misorientation angle [13, 43,63,87]. While these various reports do consistently show different results for low vs. high angle GBs, the trends at high angles are highly variable between the different reports, which could be attributed to the comparison of different materials or different sets of GB types. Finally, most involve small samplings of GBs, likely due to the difficulty in experimental measurement of GB enrichment in a large population of GBs.

It is not clear at this point whether the various sources of information are in conflict or in support of the results presented here. It is certain that at least some of the differences between the reports should be attributed to different materials, structures, and their segregation tendencies. But the variation due to GB type could be a sign that there are local but not global trends in GB concentration as indicated by the present work. Additional experiments will be required to verify whether their limited data is representative of broader global trends or whether they have extracted local trends.



Fig. 11. Concentration of solute at the GB, c_{GB} , as a function of GB excess volume and GB energy. The following are projected onto their corresponding planes: c_{GB} vs. GB energy (green), c_{GB} vs. GB excess volume (orange), and GB excess volume vs. GB energy (blue). (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

Table 5

Estimate, standard error (SE), and *p*-value of variables of the following linear model used to predict c_{GB} in at.%: $c_{\text{GB}} = x_0 + x_1 \cdot \gamma + x_2 \cdot V_{\text{exc}} + x_3 \cdot \theta_{\text{dis}}$.

Variable	Estimate	SE	<i>p</i> -value
<i>x</i> ₀	7.08	0.496	1.33×10^{-45}
<i>x</i> ₁	0.175	0.00154	0
<i>x</i> ₂	-142	1.63	0
<i>x</i> ₃	0.00504	0.00410	0.220

To determine whether we have missed a possible global low vs. high angle GB characterization often reported in the literature, we fit $c_{\rm GB}$ as a function of disorientation angle for GBs with angles less than 15°. These fits are provided in Supplemental Figure S18 where it can be seen that R^2 values for the low angle fits are all less than 0.3. This is insufficient to verify a global low vs. high angle trend, so once again, it may be that there are local but not global trends even in this simplified characterization. The slightly better fit in the fixed width GB atom selection once again highlights the need to further understand the effect of GB atom selection. More importantly, more low angle data would be required to definitively say that the computational data does or does not match the experimental observations; only 6 unique misorientations over 250 boundary planes exist in the Al dataset.

However, given that $c_{\rm GB}$ and the segregation energy spectrum do appear to correlate with GB energy and GB excess volume at the local scale, as illustrated in this work by the [111] symmetric twist GBs in Fig. 8 and by others [27,57,65,87–89], we examine these correlations further. In addition, segregation energies appear to be correlated with GB energy across the whole dataset as illustrated in Fig. 6. This is supported by observations from Huber et al. in their exploration of $\Sigma 5$ GBs, who found that segregation energy per site depended on excess volume and coordination number at the site.

Given these apparent correlations, we created a simple linear model to predict c_{GB} . We include disorientation angle to search for possible crystallographic dependence as well as two variables known to correlate with segregation, GB energy and GB excess volume. A plot of these variables, excluding disorientation angle, is shown in Fig. 11. The linear model is given in Table 5. The model has an R^2 value of 0.642 and a root mean squared error (RMSE) value of 0.043 at.%. In contrast, a linear model of $c_{\rm GB}$ as a function of GB energy alone, shown in Supplemental Figure S7, has an R^2 value of 0.271. A plot of $c_{\rm GB}$ vs. disorientation angle is shown in Supplemental Figure S18 to confirm the lack of a global correlation with $\theta_{\rm dis}$ found in the model; the *p*-value on the coefficient is 0.217.

Fig. 11 and the linear model given in Table 5 confirm the previously shown dependence of segregation on GB energy, γ , and GB excess volume, $V_{\rm exc}$, for GBs sampled over the entire 5D space. However, the linear model for $c_{\rm GB}$ has almost no dependence on the disorientation angle, $\theta_{\rm dis}$.

This lack of a relationship with the disorientation angle as well as the rugged landscape in 5D space shown in Fig. 9 make it difficult to understand how to optimize GB segregation energy characteristics through texture control or GB engineering. It may be that sufficient advantage can be obtained through traditional GB engineering efforts to obtain large populations of low-angle GBs or Σ 3 and other special CSL GBs to obtain enhanced properties, as in [43,54,87]. GB engineering for segregation through the use of other types of boundaries remains a challenge to be solved.

5. Conclusions

In this work, we examined grain boundary segregation energy spectra of Co in 7272 Al GBs that comprehensively sample the 5D space of crystallographic character. This included calculating segregation energies for more than 70 million possible sites.

Verification of the dataset involved determining how to identify bulk vs. GB atoms. While aCNA is often used for bulk determination in GBs, the number of non-negligible segregation energies that were excluded by aCNA categorization caused us to consider CSP as an alternative, with a cutoff of 0.1 for bulk determination. The differences between these two methods are illustrated in Figs. 1 and 2 and discussed further in Supplemental Section S1. The resulting segregation energy spectra from both methods were also compared in Figs. 4. 5 and 8b. It was determined that they give similar answers despite the reduced number of atoms included by aCNA, as illustrated in a comparison of c_{GB} values calculated using both CSP and aCNA shown in Supplemental Figure S16. However, the small differences point to a need for the community to address GB atom selection when examining segregation energy spectra and consider possible alternatives such as a fixed width approach, which best matches the low disorientation angle c_{GB} expectations (cf. Supplemental Figure S18). Such efforts by the community may help determine the optimal approach to extracting segregation energy distributions from both bicrystal and polcrystalline simulations. Verification also involved removing invalid segregation energy calculations that did not converge to 0 eV at large distances from the GB, since they do not match the expected behavior [62,63], and GBs with unreasonably low segregation energies. The complete list of GBs excluded from analysis in this work is given in Supplemental Table S3.

Validation involved comparing the computed GB segregation energies to similar bicrystal and polycrystal computational studies. In Fig. 4 it was shown that a subset of the data produced in this work is similar to the work of Huber et al. in [31]. The aggregated spectrum of segregation energies in the Homer bicrystal GB dataset is also similar to the segregation energy spectrum in polycrystals obtained by Wagih et al. in [27], as shown in Fig. 5 and Table 1. Both validation comparisons are favorable, but some minor differences between the polycrystal and bicrystal spectra raise a number of questions, posed in Section 3.2.2, that are worth resolving and that could impact the quality of an aggregate segregation energy spectrum.

Several insights arose from different methods of analysis. Fig. 6 shows that as GB energy increases, Co segregation in Al GBs becomes more favorable. This is supported by the increase of c_{GB} with GB energy shown in Fig. 7b, Fig. 11, and Supplemental Figure S17. Additionally,

all of the GBs have higher $c_{\rm GB}$ than $c_{\rm bulk}$, except the [111] symmetric twist perfect twin GB. Fig. 7b shows that most GBs have a preference for segregation, evidenced by their proximity to the "all segregating" corner of the plot. However, there are some interesting GBs that are outliers, many of which have [100], [110], and [111] disorientation axes. The most extreme outlier is the [111] twin GB that is located at "all anti-segregating." In addition, the temperature dependence of $c_{\rm GB}$ was demonstrated in Fig. 8c, which shows that $c_{\rm GB}$ drops dramatically at higher temperatures.

In general, it was found that $c_{\rm GB}$ has smooth variation across the 5D space of crystallographic character (see Fig. 9 and Supplemental Figure S19). Additional examination confirmed that $c_{\rm GB}$ can be described in a linear model with GB energy and GB excess volume (see Fig. 11 and Table 5), which finds no correlation with disorientation angle (see Supplemental Figure S18) across the 5D space. $c_{\rm GB}$ does not have an obvious functional form in 5D crystallographic space, which is shown by the rugged landscapes in Fig. 9 and the lack of obvious trends in Supplemental Figure S19. This emergence of local but not global trends may or may not align with the limited experimental datasets available in the literature, as discussed above; additional data will be required to verify such conclusions.

CRediT authorship contribution statement

Lydia Harris Serafin: Writing – review & editing, Writing – original draft, Visualization, Validation, Methodology, Investigation, Formal analysis, Data curation, Conceptualization. Ethan R. Cluff: Writing – review & editing, Formal analysis, Data curation. Gus L.W. Hart: Writing – review & editing, Writing – original draft, Supervision, Funding acquisition, Formal analysis, Conceptualization. Eric R. Homer: Writing – review & editing, Writing – original draft, Visualization, Validation, Supervision, Funding acquisition, Formal analysis, Conceptualization.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Data availability

The datasets for the current study are available in the Mendeley Data repository. The GB structures analyzed in the study are available at https://doi.org/10.17632/4ykjz4ngwt (Homer et al., 2022 [52,53]) and the dataset containing all of the per GB quantities computed in this work, including the $c_{\rm GB}$ values and a histogram of each GB's segregation spectrum, is available at https://doi.org/10.17632/rf3bt5f4hd (Serafin et al., 2024) [74].

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Appendix A. Supplementary data

Supplementary material related to this article can be found online at https://doi.org/10.1016/j.actamat.2024.120448.

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